

# Safety Certification for Learning-Based Control



Technical University of Munich

TUM School of Computation,  
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Chair of Robotics, Artificial  
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Systems

## Background

Superior control performance is typically achieved by using sophisticated control algorithms, which require fine-tuned parameters. Also, learning-based control schemes have recently attracted a lot of interest and have been successfully applied to robotic systems [3]. However, in applications such as autonomous driving or human-robot collaboration, ensuring safety is paramount when applying these performance-oriented controllers.

Due to the complexity of these performance-oriented controllers, verifying safety is usually very challenging. Combining a safe backup controller with a given performance-oriented controller is a powerful yet simple approach to tackle this challenge: If required, the safe backup controller is used to modify desired performance-oriented control inputs in a minimally invasive way. Thereby, safety can be ensured without overly compromising performance. This approach has been applied in various domains such as safe reinforcement learning [10, 2], human-in-the-loop control [7] or motion planning for autonomous vehicles [8].

## Description

In our previous work [9], we proposed an algorithm for filtering potentially unsafe inputs for nonlinear systems. At the core of this algorithm is the computation of a set of initial states that can be safely steered into a given target set. If the control input proposed by the performance-oriented controller keeps the system within reach of the target set, the proposed control input is applied. Otherwise, we override this control input by a safety-preserving control input.

However, the computation of the initial set in [9] relies on linearizing the nonlinear system and linear control laws which can lead to conservative results [4] that might overly compromise the resulting control performance. Therefore, the goal of this thesis is the extension of the algorithm in [9] to polynomial controllers [4].

All programming will be done in MATLAB and the final implementation should be integrated into our toolbox AROC [6].

This thesis provides you with the opportunity to get to know an advanced control algorithm that provides formal guarantees. Moreover, you gain/deepen your knowledge in control theory, numerical optimization, and reachability analysis, which is a tool for formal verification.

## Tasks

- Familiarization with our open-source MATLAB tool CORA [1].
- Familiarization with the control algorithms in [9, 5, 4].
- Extension of the linearization-based approach in [9] to polynomial controllers [4].
- Extension of your algorithm (from the previous step) to optimizing the initial set and the safety-preserving controller.
- Extension of your algorithm to compute non-convex initial sets.
- Comparison of the implemented algorithms using different benchmark systems from our toolbox AROC [6].
- *Optional:* Comparison of the implemented algorithms with a state-of-the-art approach, such as [11].
- Documentation of your results.

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**Advisor:**

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**Research project:**

justITSELF

**Type:**

Master's thesis

**Research area:**

Safety-preserving control, robust control, formal methods

**Programming language:**

MATLAB

**Required skills:**

Background in control theory and dynamical systems. Background in numerical optimization beneficial.

**Language:**

English, German

**Date of submission:**

2. Juni 2022

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